Flocking structures

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Flocking models

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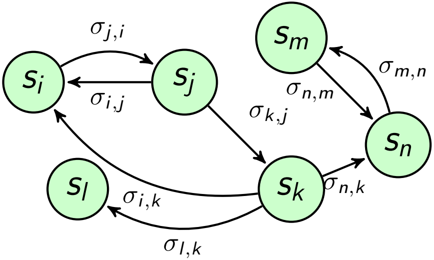
- prioritize neighbours

Dynamic networks



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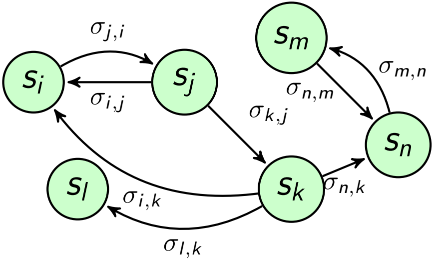

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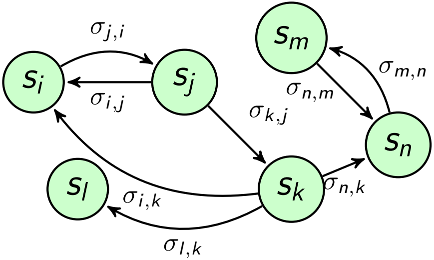

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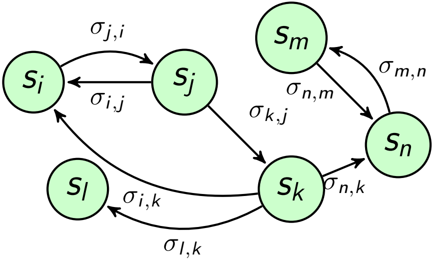

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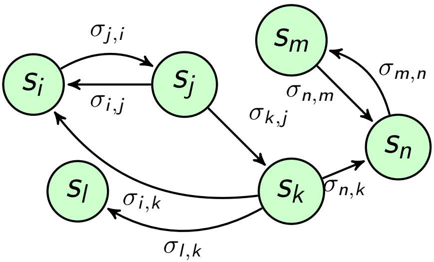

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$$\underbrace{\frac{d\sigma_{i,j}}{dt}}_{\text{gain evolution}} = \underbrace{\psi(s_i, s_j)}_{\text{state dependence}} . \qquad (2)$$

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Important parameters:

- number of agents
- number of neighbours
- ICs (spacial and communicative)

Plan

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Finish thesis