

# 3E1 Problem Sheet 17

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- Consider the network  $N$  in Fig. 1 where an edge label  $c, f$  means that the corresponding edge has capacity  $c$  and carries the flow  $f$ .
  - What is the total flow in  $N$ ?
  - Find a flow augmenting path in  $N$ ; give its vertices in order. By how much can you increase the total flow in  $N$  at most using that flow augmenting path?
  - What is the capacity of the cut set consisting of the edges  $(2, 3)$ ,  $(3, 6)$ ,  $(6, 4)$ ,  $(5, 8)$  and  $(8, 9)$ ?

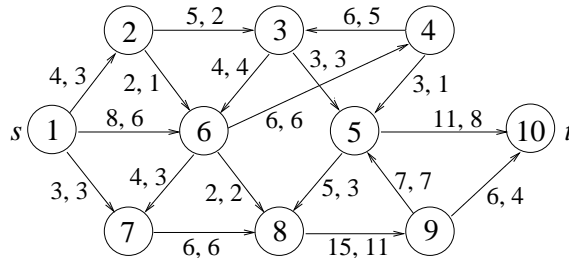


FIGURE 1

- Solve the following linear optimisation problem geometrically.  
 Maximise  $f(x_1, x_2) = 20x_1 + 30x_2$  subject to the constraints
 

(1) $4x_1 + 3x_2 \geq 12$	(2) $x_1 - x_2 \geq -3$
(3) $x_2 \leq 6$	(4) $2x_1 - 3x_2 \leq 0$
- A company produces three types of glass, flint glass ( $G_1$ ), German crystal-glass ( $G_2$ ) and crown-glass ( $G_3$ ). The amount of raw material (in  $kg$ ) needed for  $200kg$  of glass and the price per  $kg$  (in Euro), depending on the type, are given in the table below.

	sand	pearlash	arsenic	red-lead	nitre	price
$G_1$	120	35	6	40	13	35
$G_2$	120	46	6	0	7	60
$G_3$	120	60	1	0	30	70

Per day they have  $2000kg$  of sand,  $450kg$  of pearlash,  $50kg$  of arsenic,  $150kg$  of red-lead and  $180kg$  of nitre available.

Formulate a constrained optimisation problem in order to maximise the daily revenue, assuming all the glass can be sold, and transform it into normal form, by possibly introducing slack variables.